
PVPS
PHOTOVOLTAIC POWER SYSTEMS PROGRAMME
Report IEA-PVPS T2-07:2008

IEA PVPS Task 2
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Foreword

The International Energy Agency (IEA), founded in November 1974, is an autonomous body within the framework of the Organization for Economic Cooperation and Development (OECD) which carries out a comprehensive programme of energy co-operation among its member countries. The European commission and the European Photovoltaic Industry Association (EPIA) also participate in the work of the IEA.

The IEA Photovoltaic Power Systems Programme (PVPS) is one of the collaborative R&D Agreements established within the IEA. Since 1993, the PVPS participants have been conducting a variety of joint projects in the application of photovoltaic conversion of solar energy into electricity.

The mission of the IEA PVPS programme is: to enhance the international collaboration efforts which accelerate the development and deployment of photovoltaic solar energy as a significant and sustainable renewable energy option. The underlying assumption is that the market for PV systems is continuously expanding from the earlier niche markets of remote applications and consumer products, to the rapidly growing markets for building integrated and other diffused and centralised grid-connected PV generation systems. This market expansion requires the availability of and access to reliable information on the performance of PV systems, technical and design guidelines, planning methods, financing, etc. to be shared with the various actors.

The overall programme is headed by an Executive Committee composed of one representative from each participating country, while the management of individual research projects (Tasks) is the responsibility of Operating Agents. By mid 2007, twelve Tasks were established within the PVPS programme.

The overall objective of Task 2 is to improve the operation and sizing of photovoltaic systems and subsystems by collecting, analysing and disseminating information on their technical performance and reliability, providing a basis for their assessment, and developing practical recommendations for sizing purposes.

The current members of the IEA PVPS Task 2 include: Austria, Canada, European Commission, European Photovoltaic Industry Association, France, Germany, Italy, Japan, Sweden, Switzerland, United Kingdom, United States of America and Poland as an observer.

This report concentrates on the possibility of using solar irradiation calculated from satellite images for PV systems performance prediction. Comparisons have been made to irradiation measurements from systems present in the Task 2 PV Performance Database. A simple performance model has been applied to simulate the global system operation. Results are presented with their related accuracy. The technical report has been prepared under the supervision of PVPS Task 2 by:

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The report expresses, as nearly as possible, the international consensus of opinion of the Task 2 experts on the subject dealt with. Further information on the activities and results of the Task can be found at: http://www.iea-pvps-task2.org and http://www.iea-pvps.org.
Executive Summary

One of the major challenges faced by the photovoltaic industry today is to deliver secure and reliable power while managing uncertainties related, on the one hand, to fluctuations and intermittency of the energy source and on the other hand, to the full energy conversion process. Meeting the challenge requires accurate and timely information on the present and future availability of the solar resource as well as other data on parameters affecting the energy yield (close and remote shading, converters’ characteristics).

This document reports, in the first part, on the possibility to use solar irradiation calculated from satellite images for performance predictions. In the second part, different system performance evaluation models are described. The use of calculated irradiations as an input to a simple parametric model is compared with measurements from systems existing in the Task 2 Performance Database. Conclusions are drawn on the related achievable accuracy.

Remote sensing data from satellites offers an attractive and competitive approach to deliver global data sets of energy resources. Large areas of the earth’s surface can be monitored at high spatial (3x3 km²) and timely (15 minutes) resolutions using uniform and consistent methodologies. In order to make a first step forward it seemed important to compare the value extracted from the Helioclim-2 database, processed at the proper tilt and orientation angles, with some measured values on installation sites. Selected systems from the IEA PVPS Task 2 Performance Database were used as case studies. The first results have shown that in order to correctly take into account the PV system environment (in the albedo viewpoint), a fit between calculated and measured values was sometimes necessary. During spring and summer time a root mean square error (RMSE) of less than 10 % on monthly values has been achieved while 20 % was achieved during winter time. In all cases, a RMSE of less than 10 % on yearly values is observed.

Among several different system performance evaluation tools, a simple parametric model was chosen to illustrate the confidence that can be given to a simple approach predicting the output of PV systems which requires no other input data than temperature and irradiation from the HelioClim-2 irradiation database. The first results showed that to get the best results, the period used to fit the model parameters must be correctly chosen. Having taken this into account, a simple polynomial model calibrated for the selected system and monthly input data from the HelioClim-2 irradiation database could yield monthly predictions within 15 % of the measured output and with a yearly RMSE of about 10 %.
**Introduction**

The growth of domestic and large scale applications of photovoltaics (annual growth of more than 40% worldwide since 2000) demonstrates that the technology has stepped out from demonstration phases into large-scale deployment. An emerging, challenging and innovative market is currently being created. Several countries have started to exploit this huge potential as part of their future energy supply. One of the most successful instruments in developing renewable energy strategies are cost effective feed-in tariffs. Even if some countries largely encourage the integration of PV in buildings, as is the case in France, such mechanisms now also offer favourable financial conditions for large PV power stations.

To ensure the growth of the PV sector, further investigations are needed to give a certain level of security for such investments. A decision for an investment into a PV system, whatever the size, has to be carried out carefully. The main influence on the output, beside the system design, is the choice of the location and the accurate estimation of the energy generation potential.

The yield estimation has to be provided for all categories of PV systems from small configurations of 1-5 kW with an investment of several thousand euros up to a multi MW system with a total investment of several million euros.

One of the major challenges faced by the PV industry today is to deliver secure and reliable power while managing uncertainties related on the one hand to fluctuations and intermittency of the energy source and on the other hand to the full energy conversion process. Meeting the challenge requires accurate and timely information on the present and future availability of the solar resource as well as other data on parameters affecting the energy yield (close and remote shading, converters characteristics etc.).

The growth in the solar sector boosts the demand for more accurate information on performance prediction. To meet this demand, new data, algorithms, and derived products have to be developed to serve specific needs. Looking at the technical and scientific barriers, the international efforts aim at improving the maturity of data collection and processing techniques and in standardisation of derived products in order to provide the customers with optimised information.

Depending on purpose, different kinds of information are needed:

- **long term historical data sets of the expected energy yield:** to support technical feasibility studies, optimal sitting, adequate sizing, and bank audits of power plants,
- **real-time data sets on available energy resources:** to support the management of power plants and the optimisation of energy production,
- **recent, real-time and forecasted site specific irradiances:** to support the management of large dispersed PV resource throughout regional power grids as soon as the penetration of PV installations reaches a few percent,
- **local solar resource characterisation and reliable estimate on the availability of solar irradiance:** to support sensible socio-economic planning concerning the development of solar energy applications, intelligent decisions concerning the future of solar,
- **real-time data sets on weather and environmental conditions:** to support forecasting of electricity demand, which largely determines the price for buying selling and trading of electric power.
Such statistics should be based on historical data from at least 10 years time series. The data accuracy affects the success of the solar energy projects and the uncertainty in the data can make a difference between profit and loss from the investment. The climate statistics are needed by the decision makers to define appropriate support programmes that are tailored to the needs of countries and regions. Extreme meteorological events and indicators of climate change raise concerns whether the existing historical data are capable to provide accurate enough predictions of the climate for the next 20-25 years.

If we consider that system design and component behaviour are the most important factors in ensuring reaching a high performance ratio (PR), the system energy yield will nevertheless be a function of the solar irradiation level at the installation site. Thus, the performance prediction, of grid-connected PV systems is linked to a good appraisal of the solar irradiation but also to a good design of the energy conversion process.

The traditional approach of collecting solar resource data has been through field surveys and in-situ monitoring which are generally expensive and can only provide local measurements. By contrast, remote sensing data from satellites, referred to as earth observation data, offer an attractive and competitive approach to deliver global data sets of energy resources. Satellite remote sensing in combination with ground meteorological measurements and other information has become an increasingly important and effective way of developing solar resource information over large areas.

Regarding PV systems performance evaluation, a number of different methods have been developed to evaluate the performance of PV systems. Simulation codes can be used to simulate the behaviour of PV systems after having described the configuration of the installation and the related components. However, some components characteristics which are required to run a model are not easily available when the so-called components are not in the software database. Another approach, when data from a monitoring period are available for a given installation, is to consider a simple parametric model for which the parameters will be identified from existing time-series of global operational data.

The IEA PVPS Task 2 has gathered operational datasets for more than 400 systems in its Performance Database over a period of nearly ten years. This allowed some important results on the long-term performance of PV systems to be brought through the evolution in time of indicators like the PR. The influence of external parameters such as the shadowing effect, the module temperature or the behaviour of some inverters has also been highlighted. Moreover, irradiation data for many locations at different tilt and orientation angles is also part of the available data sets.

The aim of this document is to present the results obtained by using the IEA PVPS Task 2 Performance Database in the evaluation process:

- of solar irradiation using satellite data by comparison with measured values,
- of a simple parametric performance evaluation tool
- of the coupling of both approaches

to give an indication of the reachable accuracy when predicting the performance of PV systems.
1. Solar Resource Evaluation

One of the factors determining the performance of the PV system is the solar energy impinging upon the earth's surface. A significant improvement of our knowledge of the availability of solar energy resources on a global, regional up to a local level is needed to:

- contribute to setting up effective state and regional policies,
- help researchers, manufacturing industry, installing and maintenance companies to assess the performance of different PV technologies in different climatic regions,
- support other related economic sectors and increase awareness of the general public,
- assist utilities in adaptation of energy distribution networks to manage flows from multiple electricity suppliers to satisfy timely and geographically variable demand.

Therefore for proper site selection, maps of the solar irradiance components are required which can provide a reliable estimate of the average insolation. As the operation of a dense high quality measurement network is far beyond feasibility, and interpolation of terrestrial measurement does not give a realistic distribution of insolation, today it is common sense that such maps should be derived from satellite data, an approach that in principle combines spatially distributed information with fast data access.

The advantage of the satellite-based approach is that large areas of the earth’s surface can be monitored at high spatial and temporal resolutions using uniform and consistent methodologies at relatively low costs when compared to developing the same information using a ground-based network. Satellites are complementary to ground measurements; they improve the understanding of spatial distribution and dynamics of the solar resource.

Meanwhile, for mapping of solar resources several methods and services are set up, which mainly rely on satellite data.

1.1 The HelioClim Database

An objective of the École des Mines de Paris/Armines is to produce data of solar radiation, namely databases and time-series of irradiance or irradiation. These databases are produced by the processing of satellite images, especially from the Meteosat series of satellites. The databases are called HelioClim and can be accessed through the SoDa Service (www.soda-is.com), which is a web service devoted to solar radiation providing the user with solar radiation data and giving some information on possible applications and training facilities.

HelioClim is a family of databases which comprise irradiance and irradiation values. They cover Europe, Africa, the Mediterranean Basin, the Atlantic Ocean and part of the Indian Ocean. Period runs from 1985 onwards. The Meteosat data are routinely received by a receiving station at École des Mines and processed in real time. This is possible thanks to a fruitful collaboration with Meteo-France and Eumetsat. Table 1.1 describes the main characteristics of the current HelioClim databases.
Table 1.1: Main characteristics of the current HelioClim databases

<table>
<thead>
<tr>
<th></th>
<th>HelioClim-1</th>
<th>HelioClim-2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time resolution</td>
<td>Day</td>
<td>1 hour</td>
</tr>
<tr>
<td>Space resolution</td>
<td>Approx. 20 km</td>
<td>5’ of arc angle. Approx. 10 km at mid-latitude</td>
</tr>
<tr>
<td>Parameters</td>
<td>Irradiance, irradiation, global on horizontal</td>
<td>Irradiance, irradiation, global on horizontal</td>
</tr>
<tr>
<td>Update</td>
<td>None, except new versions</td>
<td>Every hour, real time</td>
</tr>
<tr>
<td>Method</td>
<td>Heliosat 2</td>
<td>Heliosat 2</td>
</tr>
<tr>
<td>Relative uncertainty (RMSE) for hourly values</td>
<td>20 – 22 %</td>
<td>-</td>
</tr>
<tr>
<td>Relative uncertainty (RMSE) for daily values</td>
<td>18 %</td>
<td>18 %</td>
</tr>
<tr>
<td>Relative uncertainty (RMSE) for monthly values</td>
<td>12 %</td>
<td>12 %</td>
</tr>
</tbody>
</table>

Table 1.2 gives the main characteristics of the HelioClim databases in preparation: HelioClim-3 should replace HelioClim-2, and should be replaced in turn by HelioClim-4. HelioClimDay should include HelioClim-1 and offer a consistent series of values from 1985 onwards.

Table 1.2: Main characteristics of the HelioClim databases in preparation

<table>
<thead>
<tr>
<th></th>
<th>HelioClim-3</th>
<th>HelioClim-4</th>
<th>HelioClimDay</th>
</tr>
</thead>
<tbody>
<tr>
<td>Period</td>
<td>Since 2004, onwards</td>
<td>Since 2004, onwards</td>
<td>Since 1985, onwards</td>
</tr>
<tr>
<td>Time resolution</td>
<td>15 min</td>
<td>15 min</td>
<td>Day</td>
</tr>
<tr>
<td>Space resolution</td>
<td>Approx. 5 km</td>
<td>Approx. 5 km</td>
<td>Approx. 5 km</td>
</tr>
<tr>
<td>Parameters</td>
<td>Irradiance, irradiation, global on horizontal</td>
<td>Irradiance, irradiation, global, direct and diffuse on horizontal, spectral distribution</td>
<td>Irradiance, irradiation, global on horizontal</td>
</tr>
<tr>
<td>Update</td>
<td>Every 15 min, real time</td>
<td>Two days delay</td>
<td>Every day, real time</td>
</tr>
<tr>
<td>Method</td>
<td>Heliosat 2</td>
<td>Heliosat 4</td>
<td>Data fusion</td>
</tr>
</tbody>
</table>

The relative uncertainty obtained on the values stored in the HelioClim databases is given in Table 1.1. The data extracted from the HelioClim-2 database, calculated at a one hour time step, have been confirmed on several sites all over Europe to bring a better accuracy than the one in the HelioClim-1. One example is given in Fig. 1.2.
1.2 Calculation at Tilt and Orientation Angles

The processing of Meteosat images gives an estimation of the global irradiance on an horizontal plane. In order to be compared with on-site measurements of the solar irradiance performed on a PV installation site, this data has to be transformed to take into account the tilt angle and the orientation of the PV generator.

There are a few algorithms which allow the split of the global irradiance into its direct and diffuse components and then make the combination of their contribution to the tilt and orientation. The higher the time resolution, the more accurate the results will be. At present, time resolution is one hour with HelioClim-2, and in the near future, will be 15 minutes with HelioClim-3. The algorithmic chain used to calculate from the horizontal to the tilted and oriented plane is given in the most recent version of the European Solar Radiation Atlas.

It is very difficult to validate the algorithmic chain used in the SoDa processor with measured data, as both global horizontal and tilted solar irradiance are rarely available for the same site. The only possible comparison can be made with the same type of processors used in well known and widely used software.

Fig. 1.2 and Fig. 1.3 show the results obtained with the SoDa and the RETScreen software on two different locations:
In each case, the relative difference between the data calculated by each software is less than 2%.

### 1.3 Comparison with Solar Irradiation Measured On Site: Evaluation of the Achievable Accuracy

In order to evaluate the confidence that can be attributed to the solar irradiation values coming from the HelioClim-2 database processed at tilt and orientation angles, comparisons have been conducted with systems stored in the IEA PVPS Task 2 Performance Database. As the HelioClim-2 one hour time step database is only available since February 2004, it has been compulsory to select some systems in the Performance Database for which detailed operational data were available from that date onwards.

Three systems have been selected:

- the Soleil Marguerite system: 13 kW installed at Villeurbanne (tilt: 30° full South)
- the Munich Trade Fair Centre: 1 MW installed at Munich (tilt: 28° full South)
- the F1 system: 1 kW rooftop installed at Lyon (tilt: 17°, 30° South West).

For each of these systems the comparison has been made on a daily basis allowing for the calculation of the root mean square error (RMSE) for monthly values and for yearly values based on monthly means.
Soleil Marguerite PV System

Detailed data, every quarter of an hour, was available for the year 2004 and monthly means have been delivered for 2005 and 2006.

The processing of detailed data for 2004 made it possible to correct the HelioClim-2 values in order to fit the best with the on-site measured values. This correction step is necessary only at times. Fig. 1.4 illustrates the difference between measured and calculated values and Fig. 1.5 shows the correction which was drawn from the comparison of the data at the daily level. A linear relationship is enough for such a correction. As the discrepancy between measured and calculated values differs for sites exhibiting similar solar climates, it is believed that the major cause for differences at Soleil Marguerite comes from the difficulty to catch the specific value of the site albedo. The albedo value is very sensitive to the installed system environment and it is difficult to take into account the real environment of an installation with a 10 km x 10 km space resolution, especially in urban conditions. Fig. 1.6 gives a view of the urban environment of this installation.

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**Fig. 1.4:** Comparison of the solar irradiation processed from the HelioClim-2 database and the solar irradiation measured on site on the tilted plane for the year 2004.

**Fig. 1.5:** Relationship between measured and calculated daily values in order to apply a correction on the HelioClim-2 data for this site.

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The correction has been applied to the HelioClim-2 data for 2004 leading to the results presented in Fig. 1.7 in terms of solar irradiation and in Fig. 1.8 in terms of RMSE monthly and yearly values. Fig. 1.9 and 1.10 show the comparison at the daily basis for the best and the worst months.

Fig. 1.7: Comparison of the solar irradiation processed from the HelioClim-2 database, corrected according to the relationship given in Fig. 1.5, and the solar irradiation measured on site on the tilted plane for the year 2004.

Fig. 1.8: RMSE calculated at the monthly level from daily data and at the yearly level from monthly means.
The correction calculated for 2004 was applied for the years 2005 and 2006 for which only monthly means were available. The results are presented in Fig. 1.11 for 2005 and in Fig. 1.12 for 2006. The RMSE on yearly values is respectively about 7% and 6% for 2005 and 2006.
**F1 PV system**

F1 is a roof integrated system (Fig. 1.13) for which detailed measured data were only available for 2004.

As the F1 PV installation is located in the same region as the Soleil Marguerite one, the same correction was applied to the HelioClim-2 solar irradiation data, giving the results shown in Fig. 1.14 and 1.15 regarding the RMSE on monthly and yearly values. Fig. 1.16 and 1.17 give an illustration of the difference on the daily basis for the best and the worst month, in terms of accuracy.

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**Fig. 1.13**: General overview of F1 system and of its roof integration with PV tiles.

**Fig. 1.14**: Comparison of the solar irradiation processed from the HelioClim-2 database, corrected according to the relationship given in Fig. 1.5, and the solar irradiation measured on site on the tilted plane for the year 2004.

**Fig. 1.15**: RMSE calculated at the monthly level from daily data and at the yearly level from monthly means.

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Fig. 1.16: Comparison of the daily solar irradiation processed from the HelioClim-2 database and the daily solar irradiation measured on site on the tilted plane for June 2004.

Fig. 1.17: Comparison of the daily solar irradiation processed from the HelioClim-2 database and the daily solar irradiation measured on site on the tilted plane for November 2004.

Munich Trade Fair Centre Photovoltaic system

This is a 1 MW roof integrated photovoltaic system (Fig. 1.18).

Detailed data on an hourly basis were available for the years 2002, 2003 and 2004. Thus, the comparison could only be made for 2004. Fig. 1.19 shows the results obtained without any corrections with the related RMSE on monthly and yearly values in Fig. 1.20.
In this case, no correction has been applied to the satellite data. The albedo value, calculated from satellite images, seems very representative of a site which does not suffer from its environment. Here also, Fig. 1.21 and 1.22 give the comparison of the solar irradiation values for the best and the worst months in terms of accuracy.

The RMSE values obtained during the winter period are much higher for this system than for the two systems installed in the Lyon region. This could come from periods of clear sky with a snow cover which the satellite interprets as a cloudy period. A representative example is shown in Fig. 1.22 between the 13th and the 19th and the 29th and the 31st of December 2004.
1.4 Comments and Further Steps

Remote sensing data from satellites offer an attractive and competitive approach to deliver global data sets of energy resources. Large areas of the earth’s surface can be monitored at high spatial and temporal resolutions using uniform and consistent methodologies. If it is agreed that such data will become more and more widely used to evaluate the potential of a site or to predict the performance of an installation for different purposes such as maintenance or energy optimization, it seems important to quantify their related accuracy and to develop procedures able to give some reliable interval of confidence.

In order to make a first step forward, it was important to compare the value extracted from the HelioClim-2 database, processed at the proper tilt and orientation angles, with some measured values on installation sites. The IEA PVPS Task 2 Performance Database was used to identify systems for which detailed data sets were available during the convenient period of time to make such an analysis possible.

The first results have shown that:

- A correction of the HelioClim2 data is necessary in order to better take into account the albedo value of the corresponding installation site, namely in case of an urban environment.
- The correction applied to a particular site, calculated over a period of time, one year in this case, can be considered as representative of the site and be applied for any other period.
- A RMSE of less than 10 % on yearly values is feasible.
- At the monthly level, a RMSE of less than 10 % can be obtained for sunny periods (spring and summer). For covered seasons, like winter, a 20 % RMSE seems more realistic at the expense of identifying snowy periods when the satellite is not able to calculate the correct site albedo.

These first very satisfying results deserve to be validated on several other sites. The correction to be applied has been determined over a one-year-period. It would be interesting to check if it is possible to reduce this period of adaptation from one year to a few months. Then it seems realistic to replace irradiance measurements by satellite data.
2. PV System Performance Prediction

The PVPS Task 2 Performance Database contains an impressive number of analytically monitored PV sites, which provide additional, relevant insolation values in sufficient time-density and continuity. This chapter aims to investigate what can be readily achieved in terms of PV system performance prediction by using the IEA PVSP Task 2 Performance Database and a model adapted to the type of data at hand. In order to illustrate the confidence that can be given to this approach, the analysis was made for two of the systems previously cited in chapter 1 for which corrected solar irradiation values coming from the HelioClim-2 database are available:

- the F1 system: 1 kW rooftop installed in Lyon, France,
- the Munich Trade Fair Centre: 1 MW installed in Munich, Germany.

For each of these systems, the comparison was made on a daily basis allowing for the calculation of the root mean square error (RMSE) for monthly values and the RMSE for yearly values based on monthly means.

2.1 Polynomial Regression Model

A number of different models are presented in Annex C. From these models, a generic polynomial regression model was chosen to simulate the performance of the selected PV systems due to the large amount of operational data already monitored and the lack of availability of many fundamental parameters required by some of the more complex models. This section describes the modeling procedure.

The model consists of a polynomial fit to operational data where the power produced by the system is a function of the incident global irradiance in the plane of the array and the PV array module temperature described by this equation:

\[ P = A + B \cdot T_{\text{module}} \cdot H_i + C \cdot H_i + D \cdot H_i^2 \]  (1)

where: 
- \( T_{\text{module}} \) is the PV array module temperature,
- \( H_i \) is the incident global irradiance,
- \( A, B, C \) and \( D \) are polynomial constants determined by least square fits.

The simulation procedure requires first the calibration of the model to the system under study in order to obtain the polynomial constants that best represent the behaviour of the system. Once the model is well adjusted, the same constants are used along with new temperature and irradiance inputs to predict the power generated by the system. Figure 2.1 shows an example of the curve fit made to the operational data of the F1 PV system in Lyon presented in chapter 1.
2.2 **PV Performance Prediction from Daily Data**

The polynomial model was used along with solar irradiation values from the HelioClim-2 database and measured data from the IEA PVPS Task 2 Performance Database to make performance predictions for selected systems. The comparison between model predictions and measured data were made on a daily basis in order to calculate the root mean square error (RMSE) for monthly and yearly values based on monthly means.

Figure 2.2 compares the monthly AC power production figures for the F1 PV system in 2004. As the HelioClim-2 one-hour time step database is only available from February 2004 onwards and the system performance data extends from January to December 2004 with one missing month (July 2004), the model was calibrated using daily measured data from February to April 2004 and predictions were made with the rest of the data (May to December with the exception of July). The measured data is represented by the black curve and the model fit to the data by the blue curve. For the period extending from April to December 2004, the red curve represents the model predictions using measured temperature and measured daily irradiation data as inputs and is an indication of the error introduced by the model alone (free of the uncertainty associated to the HelioClim-2 irradiation data). The green curve represents the forecasts made using the calibrated model and daily HelioClim-2 irradiation data. The HelioClim-2 input data were first corrected for the site of the PV system using the same methodology as what was presented in section 2.2.
Fig. 2.2: Comparison of the F1 PV system power production predictions using daily measured irradiation and daily HelioClim-2 irradiation inputs.

The monthly percentage deviations for the model alone were within 13 % and within 9 % for the whole period under study (May-Dec 2004). When HelioClim-2 daily inputs are used, the percent deviation increases to within 24 % on a monthly basis and within 22 % for the period under study (May-Dec 2004).

Figure 2.3 shows the RMSE values for the model predictions for each month calculated from daily measured and predicted results. These values typically range between 7 to 16 % and, as expected, increase to 14 to 25 % when HelioClim-2 data are used. Larger error percentages are also obtained for months with lower irradiation values (November and December). This highlights the difficulty of simulating irradiation and PV system performance under low light conditions where additional non-linear effects (spectral effects, increased charge carrier recombination losses) come into play.
Fig. 2.3: Monthly RMSE error for the F1 PV system power production predictions using daily measured irradiation (model) and daily HelioClim-2 irradiation inputs (model + HelioClim-2).

Furthermore, the F1 PV system is a roof integrated system using PV modules as tiles (see Fig. 2.4). Performance analysis showed a decrease of the performance ratio (PR) in summer due to a high cell temperature (see Fig. 2.5). As the parametric model was calibrated using winter months (February to April 2004), it was not able to anticipate the low summer performance observed for August and this is reflected in the RMSE value for August.

Fig. 2.4: Picture of the F1 PV system near Lyon and its PV roofing tiles.
Fig. 2.5: Performance analysis for the F1 PV system showing high cell temperature in August and its impact on the performance ratio of the system (from PV-Starlet project NNE5-302-2001).

Figure 2.6 compares the daily predictions made for the months of June (a), the month with the lowest RMSE, and November (b), a month with fine model prediction capabilities that were spoiled once HelioClim-2 irradiation inputs with large RMSE are used. This stresses the importance of accurate radiation forecasts for the performance prediction of PV systems.

Fig. 2.6: Comparison of daily measured data with daily predictions made for the months of June (a) and November (b).
2.3 PV Performance Prediction from Monthly Data

The analysis presented in the previous section was based on daily data. However, the majority of the data contained within the IEA PVPS Task 2 Performance Database is provided in a monthly format. Moreover, ambient and module temperature are not always available. This section focuses on the assessment of power predictions based on monthly irradiation data only.

The polynomial model is used this time with monthly data from the Munich Trade Fair Center PV system contained in the IEA PVPS Task 2 Performance Database along with corresponding site-corrected solar irradiation values from the HelioClim-2 database. As monthly data represent a smaller dataset than daily data, the calibration period for this analysis varied between 1 to 3 years using 2000-02 data. Year 2004 was used to test the predictions.

Figure 2.7 compares the measured monthly AC power production data with the values obtained from the polynomial model that has been calibrated for periods of one year using 2002 data, two years using 2001-02 data, and three years using 2000-02 data. While intuitively we are led to think that using a longer period for calibration would lead to a model that yields better results, it is not the case here. The monthly percentage deviations for all three models were within 11% and the yearly RMSE was within 6-10%. Year 2001 must have been an untypical year for the performance of this system while year 2002 must have been close to that of 2004.

![2004 Monthly Power Prediction for MTFC](image)

Fig. 2.7: Comparison of the Munich Trade Fair Centre PV system power production predictions for polynomial models calibrated under different time periods.

With this result in mind, the power production of the system was modeled using the polynomial model calibrated with one year of data along with monthly summed HelioClim-2 irradiation data available for the site. In agreement with the good correspondence between the HelioClim-2 data and the measured data observed for Figure 1.16, Figure 2.8 shows that the HelioClim-2 irradiation data does not introduce a large error in this case.
Fig. 2.8: Comparison of the Munich Trade Fair Centre (MTFC) PV system power production predictions using monthly measured irradiation and monthly HelioClim-2 irradiation inputs.

On a monthly basis, the percentage deviations were within 11% for the model predictions made from measured irradiation input data and within 15% the model predictions made from HelioClim-2 irradiation input. The RMSE values for the year under study was 6% and 7% for the model predictions using measured and Heliclim2 irradiation input.

Fig. 2.9: General overview of the Munich Trade Fair Centre roof integrated PV system ( Courtesy of Solarenergieförderverein Bayern e.V.).
2.4 Comments and Further Steps

As the interest of PV stakeholders in PV system performance prediction grows for an increasing number of applications, it becomes relevant to investigate the type of support the Performance Database of PVPS Task 2 can provide. Selected systems from the Performance database were used as case studies to illustrate the confidence that can be given to a simple approach predicting the output of PV systems requiring no other input data than what is already available within the Performance and the HelioClim-2 databases.

The first results showed that a simple polynomial model calibrated for the selected system and daily input data from the HelioClim-2 irradiation database could yield monthly predictions within 24 % (22 % on an annual basis) of the measured PV system output with monthly RMSE values ranging from 14 % to 55 % (17 % for the annual value). As the vast majority of the datasets from the Task 2 database contain data compiled on a monthly basis, a similar study was conducted on another system using monthly input data. The results yielded monthly predictions within 15 % of the measured monthly output and within 7 % for the yearly output.

The analysis stressed the importance of the accuracy of the irradiation input data and revealed the limitations of the simple polynomial model and the HelioClim-2 irradiation database for months with low insolation values. Although the approach taken yields interesting results given its simplicity, it may not meet the needs of sophisticated stakeholders who require PV system output predictions to fall within 5 % of the actual output. Further work would be required to assess the potential of the Task 2 Performance Database for performance predictions on well characterized PV systems.
Conclusion

Delivering secure and reliable power while managing uncertainties related to fluctuations and intermittency of the energy source as well as to the full energy conversion process is one of the major challenges faced by the PV industry today. Meeting this challenge requires accurate and timely information on the present and future availability of the solar resource as well as other data on parameters affecting the energy yield of PV systems. Remote sensing data from satellites offer an attractive and competitive approach to deliver global data sets of energy resources. Large areas of the earth’s surface can be monitored at high spatial and temporal resolutions using uniform and consistent methodologies. As such data will become more and more widely used to evaluate the potential of a site or to predict the performance of an installation for different purposes such as maintenance or energy optimization, it seemed important to quantify their related accuracy and to develop procedures able to give some reliable interval of confidence.

As a first step, values of irradiation from the HelioClim-2 database were processed and compared to field data contained in the IEA PVPS Task 2 Performance Database. The first results have shown that an RMSE of less than 10 % on yearly values was reachable if the HelioClim-2 data could be corrected from measured data on the same site. During spring and summertime an RMSE of less than 10 % on monthly values has been achieved while 20 % was achieved during winter time with corrected values.

In a second stage, selected systems from the Performance database were used as case studies to illustrate the confidence that can be given to a simple approach predicting the output of PV systems which requires no other input data than temperature and irradiation from the HelioClim-2 irradiation database. The first results showed that a simple polynomial model calibrated for the selected system and monthly input data from the HelioClim-2 irradiation database could yield monthly predictions within 15 % of the measured output and within 7 % of the yearly output.
References


APPENDIX A: Examples of Ongoing Activities in the Field of Photovoltaic Performance Prediction

The geographical dependency and distributed nature of solar electricity generation has lead to the development of different tools able to tackle questions which, in their respective domain, require specific location dependent answers on the performance of PV systems.

Two examples are given below to highlight the type of on-going activities in the field of PV performance prediction considering the whole problem through different aspects: a global analysis approach (PVGIS), and a performance check and error detection service (PVSAT-2).

A. 1 PVGIS

Since 2002, the Photovoltaic Geographic Information System (PVGIS) has been developed at the Joint Research Centre of The European Commission. This tools combines the long-term expertise from research laboratory, monitoring and testing with geographical knowledge.

Support systems, such as PVGIS, contribute to collecting and improving knowledge of solar energy technology that is needed in decision making. It is designed to show the geographical diversity of the solar energy resource and the aspects of distributed electricity generation from solar energy systems at the continental level. As a research tool, it improves understanding of the performance of PV technology in regions of Europe.

The results show that proper appraisal of the technology has to take into consideration national and regional particularities. The current system contains only the basic information and more detailed analyses would need data with higher spatial and temporal resolution. The implementation of the HelioClim1 data (containing time series for the period 1985-2005) allows for the analysis of the variability of the solar resource by means of probabilistic approach. PVGIS brings a beneficial added value into existing systems with enhanced visualisation and integration of geographical and socioeconomic aspects. The web interface provides an access to the basic data, maps and tools to decision makers, professionals from manufacturing industry, installation and maintenance companies, and the PV owner as well as the general public.

PVGIS consists of specifically developed programmes and two databases integrated into the GIS software GRASS (http://grass.itc.it). Public access to the subset of data and tools is provided via internet using a PHP written interface:

- a Database of the European subcontinent was created from solar radiation data collected at the meteorological ground stations,
- a Database of the Mediterranean basin, Africa and southwest Asia developed in collaboration with École des Mines de Paris at Sophia Antipolis (FR) where the solar radiation was derived from the Meteosat satellite.

Nevertheless, the database from the Meteosat satellite is not fully operational regime, therefore the analyses presented relate mainly to the use of the European database where the evaluation of the solar irradiation is interpolated from ground measurements.

Some examples are presented here showing how PVGIS can be used to tackle issues on performance of PV systems such as:

- How much electricity does a PV system generate in different regions?
- What is the seasonal and regional variation of the solar electricity generation?
- How much electricity can be produced by various technology options?
- What is the theoretical potential, and how does it compare to the present use of land?
- What is the technical potential that could be exploited in the coming years?
- What are the PV generation costs, and how are they modulated by technical parameters such as system efficiency and lifetime?
- How does the PV technology fit to the needs of the present electricity generation and consumption patterns?

Estimation of PV electricity generation potential

Inclining the PV modules from the horizontal position towards south (in the northern hemisphere) increases yearly energy yield significantly. The optimal angle of the PV module is determined by geographical latitude, and the location’s share of diffuse to global irradiation. In locations with strong terrain-shadowing, the optimum orientation of the PV modules might be slightly offset towards east or west.

Fig. A.1: Optimum tilt angle of PV modules, oriented south to maximize the yearly energy yield.

Fig. A.2: Annual sum of global irradiation received by optimally-tilted PV array (kWh/m²) and the annual PV electricity generation from a typical 1 kW crystalline silicon system (kWh/kW).
This application calculates the yearly **potential electricity generation** $E$ [kWh] of a PV configuration with defined modules inclination and orientation using a formula:

$$E = 365 P_k PR H_{h,i}$$

where $P_k$ (kW) is the peak power installed, $PR$ is the system performance ratio (typical value for roof mounted system with modules from mono- or polycrystalline silicon is 0.75) and $H_{h,i}$ is the monthly or yearly average of daily global irradiation on the horizontal or inclined surface. The calculator can suggest the optimum inclination/orientation of the PV modules to harvest maximum electricity within a year.

**PV electricity potential**

![Graph showing PV electricity potential per capita](image)

Fig. A.3: Module area ($m^2$) per capita needed to satisfy 1 % of the national electricity consumption. For comparison, the dashed line represents a surface of a TV satellite dish with diameter 0.85 m.

**PV electricity costs**

As PV systems proliferate, the decision on whether to install a new system will increasingly be made on purely economic grounds and grid-connected systems have to face competition from other electricity generation means. For small domestic systems normally installed on roof tops and owned by individual persons, the comparison should be made on the basis of the end user electricity price. For larger power systems, normally with central installations and multiple owners, the comparison must be based on market pricing and cost. Since the PV generation cannot supply base load capacity, the costs in terms of the so-called peak load can be considered.
Both case studies assumed PV module lifetime of 20 years with overall system performance ratio of 0.75. These are two of the determining factors in the cost calculation of solar electricity calculation:

- Extending the expected lifetime to 30 years would consist in a monthly system cost reduction of 23%. Evidence exists that such a target is realistic.
- Increasing the today observed values to get closer to the theoretical performance ratio limits (0.88 to 0.95).

**Summary**

Support systems such as PVGIS look at the notion of performance prediction of PV systems at a global level giving information on the PV potential with a beneficial added value due to the integration of geographical and socio-economic aspects. The kind of results delivered can be used as the first step of a decision making process at a local and regional level. Then more detailed tools, especially regarding the consideration of the system operation, are necessary to enter the design phase of a project.

**A.2 PVSAT 2**

A large number of small grid connected PV systems is in operation in Europe today and a strong increase in installed capacities is expected for the coming years. Generally these PV systems range in power from 1 to 10 kW and do not include any long-term monitoring mechanism. As most system operators are not PV specialists, system faults or decreasing performance will not be recognized and the individual plant owner will face financial losses. Considering the new existing feed-in tariffs in some European countries, the cost argument becomes more and more important for plant owner as well as for the PV industry. Therefore there is a need for methods which allow for a cheap and reliable performance check of the power production of grid-connected PV systems.
Overview of the PVSAT 2 service

PVSAT 2 aims at assembling a fully automated service for both performance check and error detection. A daily surveillance should detect malfunctions, e.g. drop out of single module strings, shading by surroundings objects or inverter failures that lead to energy losses on a daily basis.

To determine the expected energy yield of a PV system, satellite data and a small number of ground based irradiance measurements give information about the solar resource at the site of the PV system. The satellite data are used because local measurements by pyranometers are costly and need periodic maintenance.

Fig. A.5: PVSAT-2 surveillance procedure.

First, surface irradiance is derived from the MSG (Meteosat Second Generation) satellite with an improved version of the Heliosat method. For MSG, the pixel size refers to a resolution of 2 km x 2 km at the ground in Europe. The irradiance values are input for a PV simulation. According to the plant description (orientation, tilt, type and configuration of the modules, type of inverter), the PV simulation determines the expected daily energy yield. The central decision support tool carries out the daily performance check. It compares the expected and measured hourly and daily energy yields for each PV system and decides on the occurrence of a failure. In the case of failure, a footprint algorithm and a failure detection routine are processed and, if a significant malfunction is identified, the operator of the PV system is informed automatically.

Experience from the PVSAT

The accuracy of the monthly sums of global irradiation gained from the Heliosat procedure is shown in Fig. A.6. Both values for the horizontal and tilted module plane are shown. The errors for the module plane have a maximum magnitude of about 10 kWh/m² (i.e., about 10 % in summer and 30 % in winter). The errors in the radiation sum are almost proportionally transferred to errors in the estimated monthly yields of the systems (Fig. A.6).
The errors of the estimated irradiation sum for the summer month could be partly traced back to problems due to the localization of the satellite pixel and the inherent inaccuracy of the satellite method due to the comparison of the spatially averaged satellite data with point data from the ground measurements. For the winter months, the analysis revealed the inaccurate performance of models that were used to recalculate the horizontal plane data to the inclined plane of the PV array. Especially the division of the global irradiance data into its direct and diffuse components causes problems.

**Combining satellite data with ground measurements**

An additional measure to improve the accuracy of the information on irradiance is the combination of the satellite data with a small amount of ground data. For this purpose the geostatistical method kriging-of-the-differences is applied (see e.g. Beyer and Wald, 1996). To validate this procedure, tests using data from the meteorological services of Germany, Ireland and Sweden were performed (Table A.1).
Table A.1: Configuration of the ground station networks used for the test of the kriging-of-differences procedure to improve the information on the irradiance.

<table>
<thead>
<tr>
<th>Data set</th>
<th>No. of stations</th>
<th>Average distance [km]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ireland</td>
<td>7</td>
<td>120</td>
</tr>
<tr>
<td>Sweden</td>
<td>10</td>
<td>160</td>
</tr>
<tr>
<td>Germany</td>
<td>32</td>
<td>67</td>
</tr>
</tbody>
</table>

The results of a cross validation for monthly data from a yearly set are given in Fig. A.8. It is remarkable that the bias can be almost completely suppressed. The root mean square error may also be reduced, but only slightly.

As important by-product of the kriging procedure, an estimate of the uncertainty of the modelled irradiance data at each site is offered. These uncertainties may now be taken into account within the error detection routine. This knowledge is a necessary prerequisite for determining the significance of deviations between the expected and the real energy yield and therefore, for the exact determination of malfunction that may have occurred. The next section gives a presentation of the error detection and decision support routine of PVSAT-2.

Fig. A.8: Results from the application of the kriging-of-differences procedure to the quality of the modelled global irradiance. The monthly relative mean bias (rMBE) and relative root mean square errors (rRMSE) for the raw Heliosat procedure and the Heliosat plus kriging procedure are given for three ground station networks (Table A.1).
Decision support system

The footprint algorithm is based on the reliable identification of the occurrence of malfunctions. For this purpose the monitored AC power $P_{\text{mon}}$ is compared with the respective simulated power $P_{\text{sim}}$. Taking into account the uncertainties of the simulated values, significant deviations of measured and simulated power are marked. The aim of the footprint algorithm is to identify typical patterns for the occurrence of the error marks depending on the type of malfunction. Error types as e.g. 'string error', 'MPP tracking error' or 'snow coverage' may be considered.

The footprint method works in two steps. The first step contains a pre-sorting algorithm that prepares the calculated and the monitored yields to take the errors from the satellite data into account. The second step is the identification of the error source.

In general, normalised signals are considered:

\[
\begin{align*}
P_{\text{sim}}/P_{\text{mon}} &= \text{simulated power/monitored power;} \\
P_{\text{mon}}/P_{\text{inst}} &= \text{monitored power/installed power.}
\end{align*}
\]

Since the individual calculated yield values with hourly time resolution are expected to be provided with large errors, the signals $P_{\text{sim}}/P_{\text{mon}}$ will be pre-sorted as interval averages $P^*$ in different domains as described below. Interval average $P^*$ shows in general a smaller variance than the variances of the individual signals. Thus, $P^*$ exhibits more stability and allows an improved detection of errors.

Summary

PVSAT 2 looks at the performance prediction of PV systems with a monitoring approach in order to ensure the user of the proper operation of the systems. Such a process is fully appropriate for small distributed systems. The extension to big power stations has to be elaborated and will need to increase the accuracy of the evaluation of the solar resource through satellite images.
APPENDIX B: The Heliosat 2 Method

The principle of the Heliosat 2 solar radiation estimation method is that a difference in global radiation perceived by the sensor aboard the satellite is due only to a change in apparent albedo, which is itself due to an increase in the radiation emitted by the atmosphere toward the sensor. Heliosat 2 is based on the fundamentals of its predecessor, the Heliosat method, that is, computation of a cloud index \( n \) from apparent albedo \( \rho_a \), ground albedo \( \rho_g \) and albedo from very bright clouds \( \rho_n \). The modification included in the current version of Heliosat has improved such features as image calibration for any change in the satellite sensor; the adoption of a clear-sky radiation model; computation of basic albedo \( \rho_a \), \( \rho_g \) and \( \rho_n \); use of the clear-sky index and the relationship between the cloud index \( n \) and the clear-sky index.

In Heliosat 2, global horizontal irradiance, \( G \), is estimated (1) using the clear sky index, \( K_C \), and global horizontal irradiance for clear skies, \( G_C \), using the ratio:

\[
K_C = \frac{G}{G_C}
\]

where \( G_C \) is calculated using the clear sky model accepted in the most recent version of the European Solar Radiation Atlas. Index \( K_C \) is related to cloud index, \( n \), by the following parametric expression:

\[
\begin{align*}
    n < -0.2, & \quad K_C = 1.2 \\
    -0.2 \leq n < 0.8, & \quad K_C = 1 - n \\
    0.8 \leq n < 1.1, & \quad K_C = 2.0667 - 3.6667n + 1.6667n^2 \\
    n \geq 1.1, & \quad K_C = 0.05
\end{align*}
\]

(2)

This study on uncertainty concentrates in the linear range, \(-0.2 \leq n < 0.8\), because most cloud situations produce a \( n \) value in it. The cloud cover index in each pixel in the image, \( n \), is estimated using apparent albedo \( \rho_a \), the albedo for the very bright clouds, \( \rho_n \), and the ground reference albedo, \( \rho_g \), expressed as:

\[
n = \frac{\rho_a - \rho_g}{\rho_n - \rho_g}
\]

(3)

The albedo necessary are evaluated using radiance received by the satellite sensor (\( L \)) and certain outside information, such as the calibration constant of the sensor itself (\( CC \)); total irradiance the satellite sensor can detect on the visible channel (\( I_0^{\text{eff}} \)); the Linke turbidity index (\( T_{\text{met}} \)) and the geographic variables that define the pixel of interest (latitude, longitude and altitude). This information is used to estimate the atmospheric contribution by its reflectance (\( R_{\text{atm}} \)) and the transmittance (\( T \)) is calculated, keeping in mind that it appears both in the path of solar radiation from the Sun to the Earth and from the Earth to the satellite sensor. Attenuation in this second path is written as \( T_{\text{sat}} \), and is estimated from the same expressions as \( T \), but applied at the elevation angle of the satellite with regard to the observer, \( \theta_{\text{sat}} \).

The ground albedo is the contribution to apparent albedo that is attributed exclusively to the Earth’s surface. Its value is selected from a series of apparent albedo following both the restrictions for acceptable threshold and for the maximum permissible change from one image to the next. Several strategies are possible to compute \( \rho_g \).
cloud index images:

\[ n = \frac{\rho - \rho_{\text{ground}}}{\rho_{\text{cloud}} - \rho_{\text{ground}}} \]

clear sky model:

\[ G_{\text{clearsky}} \]

(turbidity, sun elevation)

clear sky index:

transmission through the atmosphere

\[ k^* = G \frac{G_{\text{clearsky}}}{G_{\text{clearsky}}} = f(n) \approx 1 - n \]

**Fig. B.1:** Sketch of the Heliosat scheme to derive the global irradiance from METEOSAT images as described by Hammer et al. (2003).

New procedures like Heliosat3 will use the Meteosat Second Generation with 3 km spectrally resolved channels and additionally the broad band visible channel with 1 km nominal resolution.
A number of different methods have been developed to evaluate the performance of PV systems. Although these methods differ in their level of complexity, many present similarities in terms of the assumptions made to calculate the performance of grid-connected PV systems. Some rely on semi-empirical/parametric fits; others use physical models that take into account the effect of irradiance, temperature as well as other system losses but neglect angle of incidence and spectral effects while other approaches make no compromise and account for all known effects, thus leading to high performance accuracies at the cost of a greater complexity. The aim of this section is not to present an exhaustive list of all methods that have been developed to date, but to describe different approaches used to evaluate the performance of grid-connected systems and present some examples with their associated level of uncertainty.

C.1 Quantification of effects

The performance of a grid-connected PV system results from the performance of its components (PV modules, inverters and balance of system components) which are in turn affected by climatic factors and associated losses. The PV modules are the most critical and complex component for the evaluation of a PV system. They are most often characterized by their power rating at Standard Test Conditions (STC): 1000 W/m$^2$, 25 °C, AM 1.5. In practice however, the power delivered by the module is lower because of effects due to irradiance level, operating temperature, angle of incidence, spectral distribution of irradiance, and so on. Many studies have quantified the relative importance of these various climatic effects and the following table provides a summary of secondary effects in PV arrays, with an estimate of their effect on monthly energy production estimates. A similar table can be found in King et al. (2002).

Table C.1 – Summary of secondary effects in PV arrays

<table>
<thead>
<tr>
<th>Effect</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>Temperature</td>
<td>1 % to 10 %</td>
</tr>
<tr>
<td>Angle of incidence</td>
<td>1 % to 5 %</td>
</tr>
<tr>
<td>Spectral distribution</td>
<td>0 % to –3 %</td>
</tr>
<tr>
<td>Uncertainty in manufacturer’s rating</td>
<td>0 to 5% or more</td>
</tr>
<tr>
<td>Ageing</td>
<td>5 % over lifetime</td>
</tr>
<tr>
<td>Mismatch</td>
<td>2 %</td>
</tr>
<tr>
<td>Soil and dirt</td>
<td>0 to 15 %</td>
</tr>
<tr>
<td>Snow</td>
<td>Location dependent</td>
</tr>
<tr>
<td>Partial shading</td>
<td>Location dependent</td>
</tr>
<tr>
<td>Diodes and wiring</td>
<td>3 %</td>
</tr>
</tbody>
</table>

One of the main aspects that differentiates PV system performance models is the extent to which these factors are taken into account and the approach taken to calculate the operating temperature of the PV array and the incident irradiance falling on the surface of the array. The next sections present different types of models categorized according to the complexity of their underlying physical models.
C.2 The Simple Model

Models of this type are reduced to their simplest form and irradiation is the only parameter taken into account. The electrical power \( P \) produced by the PV system can be calculated as:

\[
P = A \cdot f \cdot E_T \cdot \eta \cdot \eta_{\text{inv}}
\]  

(4)

where \( A \) is the net area of the PV array, \( f \) the fraction of array area with active solar cells, \( E_T \) the irradiance in the plane of the array, \( \eta \) the module conversion efficiency, and \( \eta_{\text{inv}} \) the inverter (DC to AC) conversion efficiency.

The only strength of this model is its extreme simplicity. It can be useful in the preliminary stage of construction of a simulation model, or as seen in section A.1 on PVGIS, it can be used to calculate the PV potential of a particular site over a given period if the model incorporates the notion of performance ratio accounting for climatic and system losses during this period.

C.3 First and Second Order Physical Models

These models make compromises to keep the level of complexity at a manageable level while accounting for first order effects attributable to irradiance and second order effects such as temperature and other system losses (series resistance, mismatch losses, soiling, etc.). The models often include an electrical model which calculates the electrical power delivered by the PV array, and a thermal model which calculates either cell temperature, or the heat transfer from the module, or both.

**Electrical model**

Once the operating cell temperature of the module has been determined by the thermal model, it’s electrical output can be calculated. The model calculates the short-circuit current and open-circuit voltage for the irradiance and cell temperature of interest using relations based on reference conditions (irradiance 1000 W/m\(^2\), cell temperature 25 °C, air mass 1.5), and empirical temperature coefficients \( \alpha \), \( \beta \) and \( \gamma \) characterizing the module under consideration.

The model assumes that the maximum power point current and voltage, \( I_{mp} \) and \( V_{mp} \), vary proportionally to the short circuit current and open circuit voltage (this is a debatable assumption, as the fill factor is known to vary with irradiance). As a consequence, the maximum module power \( P_{mp} \) is calculated through:

\[
P_{mp} = P_{mp,ref} \left( \frac{I_{sc} \cdot V_{oc}}{I_{sc,ref} \cdot V_{oc,ref}} \right)
\]  

(5)

where \( P_{mp,ref} \) is defined as \( I_{mp,ref} \cdot V_{mp,ref} \). When the PV system uses a maximum power point tracker, the above equation is all that is needed to calculate system output.

Some models delve deeper into underlying physics of the array and model the I-V characteristics using the one diode equivalent circuit of a solar cell (or two diode model of a PV module). According to this electrical model, the following implicit relationship between voltage \( V \) and current \( I \) holds for any given irradiance and cell temperature:
where \( I_L \) is the light current, \( I_0 \) is the diode reverse saturation current, \( R_s \) is the series resistance, \( R_{sh} \) is the shunt resistance, and \( a \) is a curve fitting parameter. These five parameters are unknown, and the model endeavors to derive them from three points on the I-V curve (short circuit current, open circuit voltage, and maximum power point) using the following simplifications:

- The shunt resistance is very large, therefore the last term of eq. (6) drops.
- The light current is practically equal to the short circuit current: \( I_L = I_{sc} \)

Finally (6) provides an implicit relationship between \( I \) and \( V \) which can be solved iteratively, either to calculate the maximum power or to find the current for a given voltage.

**Strengths and weaknesses**

Models of this type have two main strengths:

- They are relatively simple to implement,
- They require only a limited number of parameters.

Parameters appearing in the electrical model, such as \( I_{sc\,ref}, V_{oc\,ref} \) and \( P_{mp\,ref} \), and coefficients \( \alpha \), \( \beta \) and \( \gamma \) are usually readily available in manufacturer’s data sheets. However, a few I-V curves at different irradiance levels are usually necessary to obtain the parameters of the one or two diode models.

On the side of weaknesses, one should mention:

- The model assumes that maximum power point current and voltage have the same dependency on cell temperature and incident irradiance as short circuit current and open circuit voltage. This is not true in practice. The fill factor is not constant; it varies with temperature and irradiance.
- The thermal models used to calculate the module operating temperature are typically only valid in the case of an open-rack mount and thus not accurate for building-integrated applications.
- The model totally ignores spectral effects, effects related to angle of incidence and other non-linear effects observed under low irradiance conditions.

**Examples and associated accuracies**

Simulation tools falling in this category include the INSEL PV simulation tool used to detect faults or power losses in PV plants, which reports a mean arithmetic error of 2 % under suitable plant monitoring conditions (Eicker et al., 2005). The RETScreen® International Clean Energy Project Analysis Software used for PV project pre-feasibility studies reports RMSE values ranging between 3.85 % and 8.89 % for their tilted radiation calculation algorithm and PV energy production differences within 5 % when suitable model parameters are selected (Minister of Natural Resources Canada, 2003). In addition to these examples, PV models included in the building simulation tools Energy Plus and TRNSYS also use similar approaches.
C.4 Complex Physical Models

Models in this category make no compromise and take into account most, if not all, phenomena affecting the output of PV systems (or PV modules or arrays). These models however require a large number of parameters which may not be readily available and can only be obtained through an extensive set of measurements. Moreover, the solar radiation input data required for the simulation is usually only available for heavily instrumented experimental sites or simply non-existent in which case it must be obtained from atmospheric solar radiation models. Thus in most cases, the interest of the model is mostly at the conceptual level, rather than at a practical one.

The Sandia model

A successful exception to this rule is the Sandia model. This model is described in King et al. (1998). Five equations are used to describe the variation of short-circuit current $I_{sc}$, open-circuit voltage $V_{oc}$, and maximum power point current $I_{mp}$ and voltage $V_{mp}$, as a function of irradiance $E$, cell temperature $T_c$, absolute air mass $AM$ and solar angle-of-incidence $AOI$ on the PV array:

\[
I_{sc} = \left(\frac{E}{E_0}\right) f_1(AM) f_2(AOI) \left[I_{sc0} + \alpha_{Isc} (T_c - T_0)\right]
\]

\[
E_e = \frac{I_{sc}}{I_{sc0}}
\]

\[
I_{mp} = C_0 + E_e [C_1 + \alpha_{Imp} (T_c - T_0)]
\]

\[
V_{oc} = V_{oc0} + C_2 \ln(E_e) + \beta_{Voc} (T_c - T_0)
\]

\[
V_{mp} = V_{mp0} + C_3 \ln(E_e) + C_4 [\ln(E_e)]^2 + \beta_{Vmp} (T_c - T_0)
\]

$E_0$ is the reference irradiance of 1000 W/m$^2$; and $T_0$ is a reference temperature for the module. $I_{sc0}$ is the value of $I_{sc}$ under 1000 W/m$^2$, cell temperature equal to $T_0$, air mass 1.5, and zero angle of incidence. $V_{oc0}$, $I_{mp0}$, and $V_{mp0}$ are the values of $V_{oc}$, $I_{mp}$, and $V_{mp}$ for $E_e = 1$ and $T_c = T_0$.

Note that the model provides only information about the characteristic parameters of the I-V curve, not about how to calculate the whole I-V curve. $I_{sc0}$, $V_{oc0}$, $I_{mp0}$, and $V_{mp0}$ are empirically determined; so are the temperature coefficients $\alpha_{Isc}$, $\alpha_{Imp}$, $\beta_{Voc}$ and $\beta_{Vmp}$, the coefficients $C_0$, $C_1$, $C_2$, $C_3$ and $C_4$, and the air mass function $f_1$ and the angle of incidence function $f_2$.

$E_e$ is an interesting dimensionless term, called the ‘effective irradiance’. It represents the part of solar irradiance that is actually useful for energy conversion, i.e. after angle of incidence effects and spectral response of the module have been taken into account. The main assumption, often verified in practice, is that $V_{oc}$, $I_{mp}$ and $V_{mp}$ are a function of $I_{sc}$ and $T_c$ only. So once spectral and incidence effects have been taken into account in equation (7), the effective irradiance can be computed through (8) and all other parameters characteristics of the I-V curve follow equations (9) to (11).

The air mass function $f_1$ is expressed as a fourth-order polynomial of the air mass, and the angle of incidence function $f_2$ is expressed as a fifth-order polynomial of the angle of incidence. The former needs to be determined for each module, and is somewhat related to the concept of spectral mismatch correction. The latter also needs to be determined for each module, although the same function may be applicable to most modules with a glass front surface.

To use equations (7)-(11), cell temperature must be calculated. In the model this is done in two steps. First, back-surface module temperature $T_m$ is determined from environmental variables using the following relationship:
The main strength of the model resides, once again, in its completeness. It strives to take into account most of the phenomena that influence the power output of a PV module. It also compares favorably with field tests. PV arrays from a variety of technologies (EFG-Si, a-Si, Si-Film, CdTe, mc-Si) have been simulated and agreement was 97 % between measured and modeled power (King et al., 1998).

On the negative side, one should note the increased complexity of the model. The model requires the experimental determination of a very large number of parameters – no fewer than 27 to be precise. No manufacturer provides that much information about their module. Sandia does make available a database of parameters for over 120 modules, however each new module needs to be tested according to their method to obtain the parameters required by the model. The correction for air mass is only partially correct, since it assumes that air mass is the dominant influence on spectral effects. This neglects the influence of cloud cover (cloudy skies tend to be more ‘blue’ than clear skies). Finally, the thermal model calculating the temperature of the array is valid only in the case of modules mounted in an open-rack structure. It may not be applicable in the case of roof-mounted modules.

Besides the Sandia Model, other complex models that are under development include the IP PERFORMANCE models and the IEC 61853 standard which consists in an energy rating procedure comprising three parts: measurements to characterize the PV module, a calculation algorithm and reference day data.

C.5 Polynomial Regression Models

As solar irradiance and temperature data are readily obtainable for many locations in the form of mean monthly global horizontal irradiation and average ambient temperatures, a performance model based on only these two parameters has great practical benefits. The main assumption of these models is that the PV system (or module) performance may be described with just two independent parameters: in-plane irradiance and module temperature. While other effects such as diffuse content, angle of incidence and spectral distribution have some effect on power output, it is assumed that they have a small impact on the final energy production.
The reason for this is that such variations are observed in early morning or late evening and thus make a small contribution to overall energy production, and these variations tend to average out over a year. This is especially relevant since other meteorological parameters (solar spectrum, diffuse irradiance, wind speed) which may be of secondary relevance to the energy yield of PV modules are typically not available. In addition, these models do not propose exact physical models, but rather use regression models or non-physical “surface fits” to fit field and test data in order to obtain calibrated models that can then be used to make predictions under similar temperature and irradiance conditions. Two such models, the Photovoltaics for Utility Scale Applications (PVUSA) and the “Performance Surface” models are described here.

Photovoltaics for Utility Scale Applications (PVUSA)

A US government and utility sponsored activity called PVUSA has developed a test method (Whitaker et al., 1997) that relates PV system performance to the prevailing environmental conditions (solar irradiance, ambient temperature and wind speed) for a variety of technologies. These dependencies are combined in equation (14):

$$ P = H_i ( A + B \cdot H_i + C \cdot T_{amb} + D \cdot WS) \quad (14) $$

where $P$ is the PV array or inverter output, $H_i$ is the plane-of-array solar irradiance, $T_{amb}$ is the ambient temperature, $WS$ is the wind speed and $A,B,C,D$ are regression coefficients. Systems and climatic conditions are monitored for several weeks and once a sufficient data set is obtained, data is filtered and fitted to obtain the regression coefficients. The uncertainty associated to this modeling method has been evaluated at 4-5 % for system operating conditions above 400 W/m$^2$ if air-mass and angle of incidence corrections similar to those of the Sandia model (see section C.4) are made.

Performance surface

This approach has been developed at JRC Ispra and relates PV module performance to module temperature and incident irradiance (Kenny et al., 2005). This method requires the indoor measurements of more than 100 I-V curves to extract $P_{max}$ for the temperature and irradiance range of interest (typically 50-1000 W/m$^2$ and module temperatures of 25-60 °C). The data is then fitted using a 3D data analysis software to obtain a function for this “power surface”. A thermal model relates the ambient temperature to the module temperature so that widely available outdoor temperatures can be used as input to energy prediction simulations. Yearly PV module energy predictions made with this method were within 5 % of the measured production.

Strengths and weaknesses of the models

Simplicity and practicality are the main advantages of these methods when a large amount of experimental data is available to characterize the PV system or module under study. The main limitations of the PVUSA model is the necessity to collect sufficient data above a certain threshold (500-750 W/m$^2$ or 400 W/m$^2$ if spectral and angle of incidence corrections are made) and over a range of temperatures and wind speeds; as well as its poor performance at low irradiance (below 400 W/m$^2$). The Performance Surface model seems to work well under all conditions, but the methodology is limited to module performance assessment and requires a large number of indoor I-V characteristics which are not necessarily at hand.